

Moles and Stoichiometry

Unit 5

Moles and Stoichiometry

Compounds

- chemical compounds are *substances* composed of two or more *elements* that are *chemically bonded* in a *definite proportion*

Examples:

H_2O and H_2O_2 are two different chemical compounds with different chemical and physical properties

Water is never $\text{H}_{3.5}\text{O}_{1.7}$

- chemical compounds can be broken down by *chemical means*

Examples:



- chemical compounds can be represented by a specific *chemical formula* and given a specific name based on the IUPAC system of nomenclature

Examples:

H_2O is water (accepted IUPAC name) or oxidane (recommended IUPAC systematic name)

CaCO_3 is calcium carbonate

Chemical names and formulas are:

- systematic (the whole world does it the same way)
- unambiguous (they tell the *exact* composition)

Types of chemical formulas:

- empirical (the smallest whole number ratio)

Example: the molecule $\text{C}_2\text{H}_4\text{O}_2$ has the empirical formula CH_2O

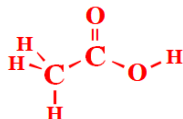
Ionic compounds all have empirical formulas, except mercury(I): Hg_2Cl_2 (See Table E)

- molecular (the *exact* composition of a molecule)

Example: the molecule glucose has the molecular formula $\text{C}_6\text{H}_{12}\text{O}_6$

- structural (shows position and bonding)

Example: the molecule $\text{C}_2\text{H}_3\text{OOH}$ has the structural formula

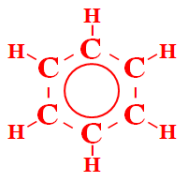


- condensed (shows position and bonding as text)

Example: the molecule $\text{C}_2\text{H}_3\text{OOH}$ has the structural formula

- skeletal (a chemical shorthand)

Example: benzene



structural



skeletal

Required by NYS Regents

Sometimes used by NYS Regents

Writing Chemical Formulas

Type-I Binary Compounds (ionic with monovalent metal)

1. Write the cation symbol first
2. Write the anion symbol last
3. If the oxidation number sum is = 0, use easy criss-cross
4. Reduce subscripts to least whole number ratio, if necessary

Notes: ammonium is treated as a monoatomic cation for naming purposes; peroxide, cyanide, and hydroxide are named as monoatomic anions (see Table E)

Example: sodium chloride

NaCl Check ox. no.s: $+1 + -1 = 0$ formula complete = NaCl

Example: magnesium chloride

MgCl Check ox. no.s: $+2 + -1 = +1$
use criss-cross $Mg^{+2}Cl^{-1} \rightarrow Mg_1Cl_2$
MgCl₂ Check ox. no.s: $+2 + 2(-1) = 0$ formula complete = MgCl₂

Example: aluminum oxide

AlO Check ox. no.s: $+3 + -2 = +1$
use criss-cross $Al^{+3}O^{-2} \rightarrow Al_2O_3$
Al₂O₃ Check ox. no.s: $2(+3) + 3(-2) = 0$ formula complete = Al₂O₃

Example: hydrosulfuric acid (acids are a special case)

HS Check ox. no.s: $+1 + -2 = -1$
use criss-cross $H^{+1}S^{-2} \rightarrow H_2S_1$
H₂S Check ox. no.s: $2(+1) + -2 = 0$ formula balanced = H₂S
H₂S always add (aq) to acid formulas formula complete = H₂S_(aq)

Type-II Binary Compounds (ionic with multivalent metal will have Roman numeral)

1. Write the cation symbol first (oxidation number already known)
2. Write the anion symbol last
3. If the oxidation number sum is = 0, use easy criss-cross
4. Reduce subscripts to least whole number ratio, if necessary

Notes: mercury(I) must occur in even numbers, e.g. Hg₂Cl₂
same notes for special polyatomic ions as for Type-I (see Table E)

Example: lead(IV) oxide

PbO Check ox. no.s: $+4 + -2 = +2$
use criss-cross $Pb^{+4}O^{-2} \rightarrow Pb_2O_4$
Pb₂O₄ Check ox. no.s: $2(+4) + 4(-2) = 0$ formula balanced = Pb₂O₄
PbO₂ Reduce subscripts, if needed formula complete = PbO₂

Type-III Binary Compounds (molecular, all nonmetal atoms, and utilizes prefixes)

1. Use the prefixes to write the formula

Example: carbon dioxide

CO adjust numbers with prefixes CO₂
CO₂ formula complete = CO₂

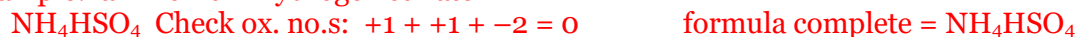
Example: dinitrogen monoxide

NO adjust numbers with prefixes N₂O
N₂O formula complete = N₂O

Polyatomic Ions (name ends with 'ate' or 'ite', use Table E)

1. Write the cation symbol first (oxidation number already known)
2. Write the anion symbol last
3. If the oxidation number sum is = 0, use easy criss-cross
4. Reduce subscripts to least whole number ratio, if necessary

Example: ammonium hydrogen sulfate



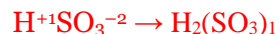
Polyatomic Acids (name ends with 'acid' but does not start 'hydro', use Table E)

1. Write the H cation symbol first (oxidation number is always +1)
2. Write the polyatomic anion symbol last
for ions ending in 'ic', search for 'ate' polyatomic ions in Table E
for ions ending in 'ous', search for 'ite' polyatomic ions in Table E
3. If the oxidation number sum is = 0, use easy criss-cross
4. Reduce subscripts to least whole number ratio, if necessary

Example: sulfurous acid



use criss-cross



Naming Compounds (Nomenclature)

Binary Compounds

1. Type-I ionic binary (metal + nonmetal, the metal is monovalent)
 - a. Write the metal name first
 - b. Write the nonmetal name last changing the ending to 'ide'

Irregular anion names:

hydrogen hydride

oxygen oxide

nitrogen nitride

phosphorus phosphide

sulfur sulfide

Example: MgCl_2

magnesium + chlorine \rightarrow chloride = magnesium chloride

Example: HCl should be a Type-III but hydrogen binaries are named like Type-I
hydrogen + chlorine \rightarrow chloride = hydrogen chloride

Example: NaCN should be polyatomic but *cyanide ions* are named like Type-I
sodium + cyanide = sodium cyanide

Example: $\text{Ca}(\text{OH})_2$ should be polyatomic but monovalent *bases* are Type-I
calcium + hydroxide = calcium hydroxide

Example: $(\text{NH}_4)_2\text{S}$ should be polyatomic but ammonium ion is named like Type-I
ammonium + sulfide = calcium hydroxide

2. Type-II ionic binary (metal + nonmetal, the metal has more than one oxidation state)
 - a. Write the metal name first
 - b. Write the metal charge (calculated from the nonmetal)
 - c. Write the nonmetal name last changing the ending to 'ide'

Example: CuO (where Cu must be +2 because O is -2)
copper + (II) + oxygen \rightarrow oxide = copper(II) oxide

Example: $\text{Cu}(\text{OH})_2$ should be polyatomic but *divalent bases* are Type-II
copper(II) + hydroxide = copper(II) hydroxide

3. Type-III binary (molecular – all elements are nonmetals, utilizes prefixes)
- Write the first element name with a prefix (never add mono to the first element)
 - Write the second element name with a prefix

List of prefixes:

- | | | |
|------------|------------|-----------|
| 1. mon(o) | 2. di | 3. tri |
| 4. ter(a) | 5. pent(a) | 6. hex(a) |
| 7. hept(a) | 8. oct(a) | 9. non(a) |
| | 10. dec(a) | |

Example: N_2O

di + nitrogen + mon + oxygen → oxide = dinitrogen monoxide

Example: CO_2

carbon + di + oxygen → oxide = carbon dioxide

4. Binary acids (molecular – H + nonmetal, must be aqueous, special naming system)
- Write the second element root name with a prefix 'hydro'
 - Add the suffix 'ic'
 - Add the name 'acid'

Binary acid root names:

- | | | |
|----------|-----------|----------|
| S sulfur | Te tellur | Se selen |
| Cl chlor | Br brom | I iod |

Example: $HCl_{(aq)}$

hydro + chlorine → chlor+ic + acid = hydrochloric acid

Polyatomic Ionic Compounds

5. Salts (Use Table E)
- Write the first element name (Type-I or Type-II)
 - Write the polyatomic ion name (from Table E)
- Example: Na_2SO_4
sodium + sulfate = sodium sulfate
- Example: $Cu(HSO_3)_2$
copper(II) + hydrogen sulfite = copper(II) hydrogen sulfite
6. Acids (Begin with H and end with a polyatomic ion, use Table E + ate-ic ite-ous)
- Write the polyatomic ion name (from Table E) changing the ending
ate → ic
ite → ous
 - Write the word 'acid'

Example: H_2SO_4

sulfate → sulfuric + acid = sulfuric acid

Example: H_3PO_3

phosphite → phosphorous + acid = phosphorous acid

Note that only phosphate (PO_4^{3-}) is shown on Table E, so (PO_3^{3-}) is phosphite

Example: $HClO$

hypochlorite → hypochlorous + acid = hypochlorous acid

7. Bases (Start with a metal and end in -OH, name like Type-I or Type-II binary)
- See examples in Type-I and Type-II ionic binaries

Organic Compounds (carbon based with special rules that we will learn in a later unit)

Finding Gram Formula Mass (gfm)

Formula Mass – the sum of the atomic masses of the atoms in a substance

- based on atomic mass, the unit is the atomic mass unit (amu or u)
 - the amu is arbitrary
 - the amu is relative ($1/12^{\text{th}}$ the mass of a C-12)
 - $1 \text{ amu} = 1.66054 \times 10^{-24} \text{ grams}$ or $6.02214 \times 10^{23} \text{ u} = 1 \text{ gram}$
 - $6.02214 \times 10^{23} = \text{Avogadro's Number } (\mathcal{N}_A)$
- the atomic mass of an element is given in the upper left corner on the Periodic Table

The Magic of Avogadro's Number – \mathcal{N}_A turns amu (or u) into grams

Example: sodium

1 atom of sodium = 22.99 g

$$22.99 \text{ u} \times 1 \text{ mole} = 22.99 \text{ g}$$

$$22.99 \text{ u} \times 6.02214 \times 10^{23} =$$

$$22.99 \text{ u} \times 6.02214 \times 10^{23} \times \frac{1 \text{ g}}{6.02214 \times 10^{23} \text{ u}} =$$

$$22.99 \cancel{\text{ u}} \times \cancel{6.02214} \times \cancel{10^{23}} \times \frac{1 \text{ g}}{\cancel{6.02214} \times \cancel{10^{23}} \cancel{\text{ u}}} =$$

$$= 22.99 \text{ g}$$

$$1 \text{ mole} = 6.02214 \times 10^{23}$$

$$6.02214 \times 10^{23} \text{ u} = 1 \text{ gram}$$

cancel terms and units

$$1 \text{ mole} = 6.02214 \times 10^{23}$$

This will always work because the number in one mole and the number of atomic mass units in 1 gram are equal

$$(1 \text{ mole} = 6.02214 \times 10^{23} \text{ and } 6.02214 \times 10^{23} \text{ u} = 1 \text{ g})$$

The gfm is always measured for a representative particle

Metals: 1 atom

Example: copper: the gfm is for Cu

Ionic compounds: 1 empirical formula

Example: sodium sulfate: the gfm is for Na_2SO_4

Network solids: 1 atom for elements or 1 empirical formula for compounds

Example: diamond: the gfm is for C

Example: quartz: the gfm is for SiO_2

Molecular solids: 1 molecule

Example: carbon dioxide: the gfm is for CO_2

Calculating the gfm

Example: CaCO_3

$$\text{Ca: } 40.08 \quad = \quad 22.99 \quad \text{u}$$

$$\text{C: } 12.011 \quad = \quad 12.011 \quad \text{u}$$

$$\text{O: } 15.9994 \times 3 \quad = \quad \underline{47.9982} \quad \text{u}$$

$$100.09 \quad \text{u}$$

(the formula mass)

$$100.09 \quad \text{g}$$

(the gfm)

Example: $\text{Al}_2(\text{SO}_4)_3$

$$\text{Al: } 26.98154 \times 2 \quad = \quad 53.96308 \quad \text{u}$$

$$\text{S: } 32.065 \times 3 \quad = \quad 96.195 \quad \text{u}$$

$$\text{O: } 15.9994 \times 12 \quad = \quad \underline{191.9928} \quad \text{u}$$

$$342.151 \quad \text{u}$$

(the formula mass)

$$342.151 \quad \text{g}$$

(the gfm)

Empirical and Molecular formulas

Empirical formula: the simplest whole-number ratio of atoms of the elements in a compound

Molecular formula: the actual ratio of atoms of the elements in a molecular compound

Empirical formula from molecular formula

1. Find the greatest common factor (GCF) of the subscripts
2. Divide all subscripts by the GCF

Example: find the empirical formula of tetraphosphorus decaoxide

Formula from name \rightarrow P_4O_{10}

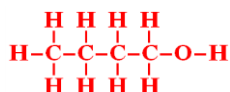
GCF of 4 and 10 = 2

$4 \div 2 = 2$ and $10 \div 2 = 5$

Empirical formula for P_4O_{10} is P_2O_5

Example: find the empirical formula of

Formula from structure \rightarrow $C_4H_{10}O$



GCF of 4, 10, and 1 = 1

Empirical formula is $C_4H_{10}O$

Molecular formula from empirical formula and gfm

The molecular formula *must* be a multiple of the empirical formula

The molecular mass (gfm) *must* be a multiple of the empirical mass

1. The gfm of the empirical formula
2. Calculate the molecular mass \div empirical mass
3. Multiply the empirical formula by the quotient from Step 2

Example: find the molecular formula of a compound that has a molecular mass of 56 u and an empirical formula of CH_2

The empirical formula (CH_2) has a gfm = $12 + 2(1) = 14$ u

$56 \text{ u} \div 14 \text{ u} = 4$

$4(CH_2) = C_4H_8$

Percent Composition

While not always explicitly stated, percent composition problems are implicitly by mass unless explicitly stated otherwise (the Regents does not do mole fraction problems)

From Table T:

$$\% \text{ composition by mass} = \frac{\text{mass of part}}{\text{mass of whole}} \times 100$$

Example: find the percent composition by mass of sulfur in sodium thiosulfate

sulfur = S

sodium thiosulfate = $Na_2S_2O_3$

sulfur = $32.065 \text{ u} \times 2$

$Na_2S_2O_3 =$

= 64.130 u

Na = $22.98977 \text{ u} \times 2$

S = $32.065 \text{ u} \times 2$

O = $15.9994 \text{ u} \times 3$

158.108 u

$$\% \text{ composition by mass} = \frac{\text{mass of part}}{\text{mass of whole}} \times 100$$

$$= \frac{\text{mass of S}}{\text{mass of } Na_2S_2O_3} \times 100 = \frac{64.130 \text{ u}}{158.108 \text{ u}} \times 100$$

$$= 40.561 \%$$

Example: find the percent composition of water in sodium thiosulfate pentahydrate

water = H₂O

$$\begin{array}{r} \text{H}_2\text{O} = \\ \text{H} = 1.00794 \text{ u} \\ \text{O} = 15.9994 \text{ u} \\ \hline = 18.0153 \text{ u} \end{array}$$

sodium thiosulfate = Na₂S₂O₃

$$\begin{array}{r} \text{Na}_2\text{S}_2\text{O}_3 = \\ \text{Na} = 22.98977 \text{ u} \times 2 \\ \text{S} = 32.065 \text{ u} \times 2 \\ \text{O} = 15.9994 \text{ u} \times 3 \\ \hline 158.108 \text{ u} \end{array}$$

$$\begin{aligned} \% \text{ composition by mass} &= \frac{\text{mass of part}}{\text{mass of whole}} \times 100 \\ &= \frac{\text{mass of H}_2\text{O}}{\text{mass of Na}_2\text{S}_2\text{O}_3 \cdot 5\text{H}_2\text{O}} \times 100 = \frac{(18.0153 \text{ u})5}{158.108 \text{ u} + (18.0153 \text{ u})5} \times 100 \\ &= 36.2942 \% \end{aligned}$$

Example: determine the mass of iron in a 75.0 gram sample of iron(III) oxide.

iron(III) oxide = Fe₂O₃

$$\text{Fe}_2\text{O}_3 = 159.687 \text{ u}$$

$$\begin{aligned} \text{mass Fe} &= \text{actual mass of whole} \times \frac{\text{formula mass of part}}{\text{formula mass of whole}} \\ &= \text{mass of ore} \times \frac{\text{mass of Fe}}{\text{mass of Fe}_2\text{O}_3} = 75.0 \text{ g}_{\text{Fe}_2\text{O}_3} \times \frac{(55.845 \text{ u})2}{159.687 \text{ u}} \\ &= 52.5 \text{ g} \end{aligned}$$

Mass Mole Problems

Using Table T

Formula for Mole Calculations:

$$\text{number of moles} = \frac{\text{given mass}}{\text{gram-formula mass}} \quad \text{or} \quad n = \frac{m}{\text{gfm}}$$

where:

<u>value</u>	<u>symbol</u>	<u>unit</u>
number of moles	(n)	= mol
given mass	(m)	= g
gram-formula mass	(gfm)	= g/mol

Changing Mass to Moles

Example: how many moles of water are represented by 5.45 grams of water?

$$\begin{aligned} n &= ? \\ m &= 5.45 \text{ g} \\ \text{gfm} &= 18.0153 \text{ g/mol} \\ n &= \frac{m}{\text{gfm}} = \frac{5.45 \text{ g}}{18.0 \text{ g/mol}} = 0.303 \text{ mol} \end{aligned}$$

Changing Moles to Mass

Example: how many grams of sodium sulfate are represented by 0.731 mol of Na₂SO₄ (gfm = 142 g/mol)?

$$\begin{aligned} m &= ? \\ n &= 0.731 \text{ mol} \\ \text{gfm} &= 142 \text{ g/mol} \\ n &= \frac{m}{\text{gfm}} = 0.731 \text{ mol} = \frac{m}{142 \text{ g/mol}} \\ m &= 0.731 \text{ mol} \times 142 \text{ g/mol} = 104 \text{ g} \end{aligned}$$

Mass Mole Problems (continued)

Using Conversion Factors

Formula for Mole Calculations:

where:

<u>value</u>	<u>symbol</u>	<u>unit</u>
number of moles	(n) =	mol
given mass	(m) =	g
gram-formula mass	(gfm) =	g/mol

Changing Mass to Moles

Example: how many moles of water are represented by 5.45 grams of water?

$$n = ?$$

$$m = 5.45 \text{ g}$$

$$\text{gfm} = 18.0153 \text{ g/mol}$$

$$n = 5.45 \text{ g} \times \frac{1 \text{ mol}}{18.0 \text{ g}} = 0.303 \text{ mol}$$

Changing Moles to Mass

Example: how many grams of sodium sulfate are represented by 0.731 mol of Na_2SO_4 (gfm = 142 g/mol)?

$$m = ?$$

$$n = 0.731 \text{ mol}$$

$$\text{gfm} = 142 \text{ g/mol}$$

$$m = 0.731 \text{ mol} \times \frac{142 \text{ g}}{1 \text{ mol}} = 104 \text{ g}$$

Chemical Reactions

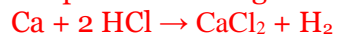
For languages we use: letters, words, and sentences

For chemical reactions we use: symbols (representing elements), formulas (representing compounds), and equations (representing reactions)

All chemical reactions exhibit:

- conservation of mass (matter is neither created nor destroyed)

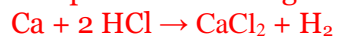
Example 1: modeling conservation of mass



Let Ca = ○, H = ⊗, and Cl = ●

When # atoms is =, the mass is =

Example 2: calculating conservation of mass



$$40. \text{ g} + 73 \text{ g} = 111 \text{ g} + 2 \text{ g}$$

The mass is = on both sides

Example 3: atom tracking



$$1 \text{ Ca } 1$$

$$2 \text{ H } 2$$

$$2 \text{ Cl } 2$$

The atom count is = on both sides

- conservation of energy (energy is neither created nor destroyed)

Example: $\text{H}^+_{(\text{aq})} + \text{OH}^-_{(\text{aq})} \rightarrow \text{H}_2\text{O}_{(\text{l})} + \text{energy}$

This example is an endothermic reaction (bond formation) but how we do not know if the PE of the ions on the left is equal to the heat released on the right

Table I shows that the amount of heat energy released should be 55.8 kJ/mol



- conservation of charge (the total charge must be the same on both sides of an equation)

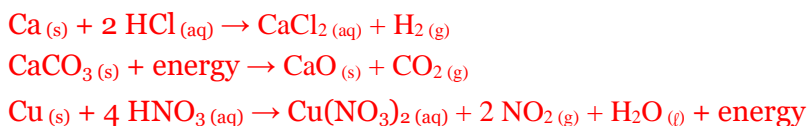
Example: Which equations represents the conservation of charge?

- (1) $\text{Cu} + \text{Ag}^+ \rightarrow \text{Cu}^{2+} + \text{Ag}$ $1+ \neq 2+$
 (2) $\text{Mg} + \text{Zn}^{2+} \rightarrow 2 \text{Mg}^{2+} + \text{Zn}$ $2+ \neq 4+$
 (3) $2 \text{F}_2 + \text{Br}^- \rightarrow 2 \text{F}^- + \text{Br}_2$ $1- \neq 2-$
 (4) $2 \text{I}^- + \text{Cl}_2 \rightarrow \text{I}_2 + 2 \text{Cl}^-$ $2- = 2-$ (this is the correct answer)

Balanced equations show:

- changes in bonding of atoms
- reactants (starting substances, R)
- products (substances that form, P)
- + signs to separate substances
- \rightarrow (yields sign) separates R and P
- coefficients (numbers) to balance atoms
- phase symbols (s), (l), (g), or (aq)

Sample balanced equations:

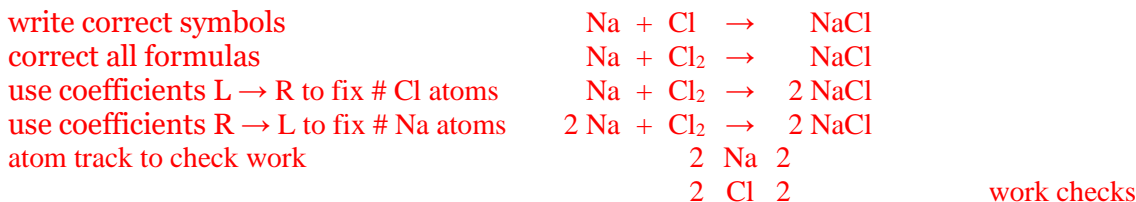


Hints for balancing equations:

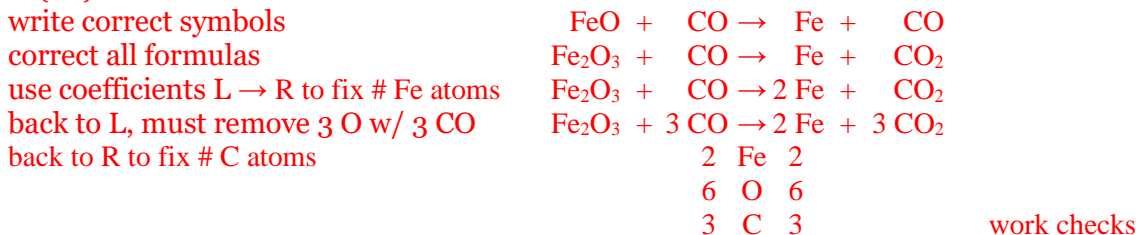
- the 'gens' are diatomic as elements
 $\text{H}_2, \text{N}_2, \text{O}_2, \text{F}_2, \text{Cl}_2, \text{Br}_2, \text{I}_2$ (How Nice Of Cleo to Bring Ice)
- start with the most complicated particle, or start with a singular occurring element, or work symmetrically left – right – left
- treat polyatomic ions as *one* thing
- if H_2O is present, balance H and O last
- check your work with atom tracking

Examples of how to balance equations:

sodium and chlorine form table salt



iron(III) oxide and carbon monoxide forms iron and carbon monoxide



Using reaction types to help balance equations:

Types of chemical reactions:

- Synthesis $A + X \rightarrow AX$
 $2 \text{H}_2(\text{g}) + \text{CO}_2(\text{g}) \rightarrow 2 \text{H}_2\text{O}(\text{g})$
- Decomposition $AX \rightarrow A + X$
 $\text{H}_2\text{CO}_3(\text{aq}) \rightarrow \text{CO}_2(\text{g}) + \text{H}_2\text{O}(\text{l})$
- Single Replacement $X + AY \rightarrow AX + Y$
 $\text{Zn}(\text{s}) + \text{CuSO}_4(\text{aq}) \rightarrow \text{ZnSO}_4(\text{aq}) + \text{Cu}(\text{s})$
- Double Replacement $AX + BY \rightarrow AY + BX$
 $\text{NaCl}(\text{aq}) + \text{AgNO}_3(\text{aq}) \rightarrow \text{NaNO}_3(\text{aq}) + \text{AgCl}(\text{s})$
- Combustion $\text{CH} + \text{O}_2 \rightarrow \text{CO}_2 + \text{H}_2\text{O}$
 $\text{CH}_4(\text{g}) + 2 \text{O}_2(\text{g}) \rightarrow \text{CO}_2(\text{g}) + 2 \text{H}_2\text{O}(\text{g})$

Examples of using reaction types to balance equations:

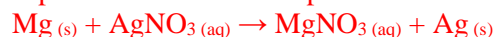
Example 1: finish then balance the following equation:



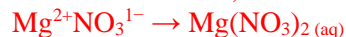
Match to generalized equation



Swap A and B to write the products



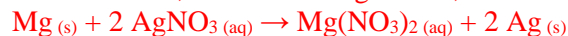
Check new formulas, use criss-cross if needed



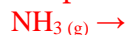
Work L→R→L, start with $(\text{NO}_3^{1-})_2$ on the right → add coefficient to left



Work L→R→L, now have 2 Ag on left, add coefficient to make 2 Ag on the right



Example 1: finish then balance the following equation:



Match to generalized equation



Decompose to A and X to write the products



Check new formulas, the 'gens' are diatomic molecules



Work L→R→L, start with N_2 on the right → add coefficient to left



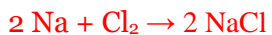
Work L→R→L, now have 6 H on left, add coefficient to make 6 H on the right



Mole and Mass Stoichiometry Problems

Conservation of Mass

Example: How many grams of NaCl can be formed by the complete reaction of 46 grams of sodium with 71 grams of chlorine?

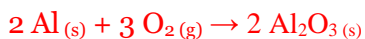


$$46 \text{ g} + 71 \text{ g} = ? \text{ g} \quad \text{The total mass is the same on both sides, } 46 \text{ g} + 71 \text{ g} = 117 \text{ g}$$
$$= 117 \text{ g}$$

Mole to Mole

Coefficients in balanced equations represent mole to mole ratios of reactants and products. The coefficients can be used as conversion factors to calculate the correct relative amounts of reactants and products to satisfy the requirements of the conservation of mass.

Example: Given the following reaction, how many moles of oxygen gas are required to completely react with 47.5 moles of aluminum metal?



$$47.5 \text{ mol Al} \times \frac{3 \text{ mol O}_2}{4 \text{ mol Al}} = 35.6 \text{ mol O}_2$$